

SEEM COLLABORATIVE
Standards for Mathematics
(CCSS)

Standards for Mathematical Practice
Grade Four

In 2012, six districts came together and began the process of creating a document that aligned our math curriculum to the Common Core State Standards (CCSS). This document is the result of that work. It features standards organized in units with key concepts and skills identified, and a pacing guide for each unit. The standards for Mathematical Practice are an integral component of the CCSS and are embedded in the units.

Each unit has the required and suggested assignments and activities for you to use in your instruction. Each unit will have required assessment pieces and a required daily math review to keep revising the content and instruction for the students. Any activity that is required must be done, but the rest of your instruction will be flexible to meet the needs of your students.

Please remember this document will be reviewed over time and after implementation. All information in these maps can also be found in our district-wide Atlas system.

This document is to give you a frame from which you teach the CCSS to your students, but allows you the freedom to instruct them how you see fit.

Grade Four Standards for Mathematical Practice

The K-12 Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. This page gives examples of what the practice standards look like at the specified grade level.

<i>Standards</i>	<i>Explanations and Examples</i>
Students are expected to: 1. Make sense of problems and persevere in solving them.	In fourth grade, students know that doing mathematics involves solving problems and discussing how they solved them. Students explain to themselves the meaning of a problem and look for ways to solve it. Fourth graders may use concrete objects or pictures to help them conceptualize and solve problems. They may check their thinking by asking themselves, “Does this make sense?” They listen to the strategies of others and will try different approaches. They often will use another method to check their answers.
Students are expected to: 2. Reason abstractly and quantitatively.	Fourth graders should recognize that a number represents a specific quantity. They connect the quantity to written symbols and create a logical representation of the problem at hand, considering both the appropriate units involved and the meaning of quantities. They extend this understanding from whole numbers to their work with fractions and decimals. Students write simple expressions that record calculations with numbers and represent or round numbers using place value concepts.
Students are expected to: 3. Construct viable arguments and critique the reasoning of others.	In fourth grade, students may construct arguments using concrete referents such as objects, pictures, and drawings. They explain their thinking and make connections between models and equations. They refine their mathematical communication skills as they participate in mathematical discussions involving questions like “How did you get that?” and “Why is that true?” They explain their thinking to others and respond to others’ thinking.
Students are expected to: 4. Model with mathematics.	Students experiment with representing problem situations in multiple ways, including numbers, words (mathematical language), drawing pictures, using objects, making a chart, list, or graph, creating equations, etc. Students need opportunities to connect the different representations and explain the connections. They should be able to use all of these representations as needed. Fourth graders should evaluate their results in the context of the situation and reflect on whether the results make sense.
Students are expected to: 5. Use appropriate tools strategically.	Fourth graders consider the available tools (including estimation) when solving a mathematical problem and decide when certain tools might be helpful. For instance, they may use graph paper or a number line to represent and compare decimals and protractors to measure angles. They use other measurement tools to understand the relative size of units within a system and express measurements given in larger units in terms of smaller units.
Students are expected to: 6. Attend to precision.	As fourth graders develop their mathematical communication skills, they try to use clear and precise language in their discussions with others and in their own reasoning. They are careful about specifying units of measure and state the meaning of the symbols they choose. For instance, they use appropriate labels when creating a line plot.
Students are expected to: 7. Look for and make use of structure.	In fourth grade, students look closely to discover a pattern or structure. For instance, students use properties of operations to explain calculations (partial products model). They relate representations of counting problems such as tree diagrams and arrays to the multiplication principle of counting. They generate number or shape patterns that follow a given rule.
Students are expected to: 8. Look for and express regularity in repeated reasoning.	Students in fourth grade should notice repetitive actions in computation to make generalizations. Students use models to explain calculations and understand how algorithms work. They also use models to examine patterns and generate their own algorithms. For example, students use visual fraction models to write equivalent fractions.

Unit Title	Pacing	Standards Major Standards; <i>Supporting Standards;</i> Additional Standards	Required Lessons	Supplements
Review – September			2.7, MJ p. 7, 1.1 2.7 Addition of Multi-digit Numbers -Enrichment 2.9 Subtraction of Multi – digit Numbers 5.3(MM) Estimating Sums	Subtraction with Borrowing
1. Understanding and Using Place Value to Multiply and Divide	5 weeks	4.NBT.1 4.NBT.2 4.NBT.3 4.NBT.5 4.NBT.6*	<u>Place Value</u> 2.2 Many Names for Numbers 2.3(millions) Place Value and Whole Numbers 2.4 Place Value with Calculators 5.8 Big Numbers 5.9*Powers of Ten *(exclude exponents) 5.10 Rounding and Reporting Large Numbers 5.11 Comparing Data 7.12(MJ, p.216) Algorithm 7&8 <u>Multiplication</u> 3.2 Multiplication Facts 3.3 Multiplication Facts Practice 3.4 More Multiplication Facts Practice 3.8* Guide For Solving Number Stories 3.9 True or False Number Sentences 5.1 Extended Multiplication Facts 5.2 Multiplication Wrestling 5.4 Estimating Products 5.5 Partial-Products Multiplication, part 1 5.6 Partial-Products Multiplication, part 2 <u>Division</u> 6.3 Partial-Quotients Division Algorithm, part 1 6.10 Partial-Quotients Division Algorithm, part 2	

2. Factors and Multiples	2 weeks	4.OA.1 4.OA.4 4.OA.5	<u>Factors & Multiples</u> 3.5 Multiplication and Division 3.11 Open Sentences 5.1 Extended Multiplication Facts 6.2 Strategies for Division <u>Patterns</u> 3.1 “What’s My Rule”	3.2 Multiplication Facts 3.3 Multiplication Facts Practice 3.4 More Multiplication Facts Practice *need supplementary materials for factors and multiples, prime and composite numbers, and patterns with numbers and shapes
3. Multi-Digit Whole Number Computation	3 weeks	4.OA.2 4.OA.3 4.NBT.4	Algorithm 1&3 (ED site) 1.3 p 7 3.6 World Tour: Flying to Africa 3.8 A Guide for Solving Number Stories 6.1 Multiplication and Division Number Stories 6.4 Expressing and Interpreting Remainders	2.7 Addition of Multi-digit Numbers 2.9 Subtraction of Multi – digit Numbers 5.3 Estimating Sums 5.5 Partial-Products Multiplication, part 1 5.6 Partial-Products Multiplication, part 2 5.8 Big Numbers 6.2 Strategies for Division 6.3 Partial-Quotients Division Algorithm, part 1 6.10 Partial-Quotients Division, part 2 8.8 Geographical Area Measurements *need supplemental materials on multi-step word problems using all operations
4. Comparing Fractions and Understanding Decimal Notation	4 weeks	4.NF.1 4.NF.2 4.NF.5 4.NF.6 4.NF.7	4.1 Decimal Place Value 4.2 Review of Basic Decimal Concepts 4.3 Comparing and Ordering Decimals 4.4 Estimating with Decimals 7.1 Review of Basic Fraction Concepts 7.6 Many Names for Fractions 7.7 Equivalent Fractions 7.8 Fractions and Decimals	*Fractions limited to denominators with 2, 3, 4, 5, 6, 8, 10, 12 and 100 4.7 Thousandths 8.3 Area (Math box) *supplemental materials needed for

			<u>Time</u> <u>Masses of Objects</u> 11.1 Weight 11.7 Capacity and Weight <u>Perimeter and Area</u> 8.1 Kitchen Layouts and Perimeter 8.3 Area 8.5 Formula for the Area of a Rectangle 8.8 Geographical Area Measurements <u>Problem solving</u> 12.2 Solving Rate Problems 12.3 Converting Between Rates 12.6 MJ, p. 326	
7. Exploring Angles and Angle Measurement	2 weeks	4.G.1 4.MD.5a 4.MD.5b 4.MD.6 4.MD.7	<u>Parts of Angles</u> 1.2 Points, Lines Segments, Lines, and Rays 1.3 Angles, Triangles and Quadrangles 1.6 Drawing Circles with a Compass 1.7 Circle Constructions <u>Measuring & Sketching Angles</u> 6.5 Rotations and Angles 6.6 Using a Full-Circle Protractor 6.7 The Half-Circle Protractor <u>Additive properties of Angle measures</u> *No Everyday Math Lesson	*supplemental materials for angles measured in reference to the fraction of the circular arc between the points where the two rays intersect the edge of the circle *supplemental materials on parallel and perpendicular lines:
8. Understanding Properties of Two-Dimensional Figures	3 weeks	4.OA.5 4.G.2 4.G.3	<u>Identify and Classifying two-dimensional shapes</u> 1.4 Parallelograms 1.5 Polygons	1.2 Points, Lines Segments, Lines, and Rays 1.3 Angles, Triangles and Quadrangles 1.6 Drawing Circles with a Compass

			1.8 Hexagon and Triangle Constructions 2.1 A Visit to Washington D.C. (Polygon Pair up) <u>Geometric Patterns</u> 10.5 Frieze Patterns* Math Masters Page 40, Project 4 Quilt <u>Line Symmetry</u> 10.1 Explorations of Transparent Mirrors 10.2 Finding Lines of Reflection 10.3 Properties of Reflections 10.4 Line Symmetry	1.7 Circle Constructions 3.2 Multiplication Facts 3.3 Multiplication Facts Practice 3.7 Finding Air Distance 6.7 The Half-Circle Protractor 12.2 Solving Rate Problems 12.3 Converting Between Rates *Supplemental materials for right triangles, acute, and obtuse angles, parallel and perpendicular lines
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Pacing: 5 weeks

Mathematical Practices

Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.

Practices in bold are to be emphasized in the unit.

- 1. Make sense of problems and persevere in solving them.**
- 2. Reason abstractly and quantitatively.**
3. Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.**
5. Use appropriate tools strategically.
- 6. Attend to precision.**
- 7. Look for and make use of structure.**
8. Look for and express regularity in repeated reasoning.

Domain and Standards Overview

Number and Operations in Base Ten

- Generalize place value understanding for multi-digit whole numbers.
- Use place value understanding and properties of operations to perform multi-digit arithmetic.

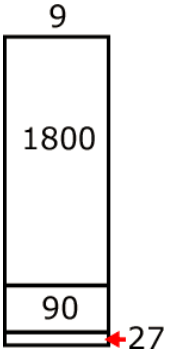
CCSS	Explanations and Examples*
<p>4. NBT.2. Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form. Compare two multi-digit numbers based on meanings of the digits in each place, using $>$, $=$, and $<$ symbols to record the results of comparisons. *</p> <p>* Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.</p>	<p>4.NBT.2. The expanded form of 275 is $200 + 70 + 5$. Students use place value to compare numbers. For example, in comparing 34,570 and 34,192, a student might say, both numbers have the same value of 10,000s and the same value of 1000s; however, the value in the 100s place is different so that is where I would compare the two numbers.</p>
<p>4.NBT.1. Recognize that in a multi-digit whole number, a digit in one place represents ten times what it represents in the place to its right. <i>For example, recognize that $700 \div 70 = 10$ by applying concepts of place value and division. *</i></p> <p>* Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.</p>	<p>4.NBT.1. Students should be familiar with and use place value as they work with numbers. Some activities that will help students develop understanding of this standard are:</p> <ul style="list-style-type: none"> • Investigate the product of 10 and any number, then justify why the number now has a 0 at the end. ($7 \times 10 = 70$ because 70 represents 7 tens and no ones, $10 \times 35 = 350$ because the 3 in 350 represents 3 hundreds, which is 10 times as much as 3 tens, and the 5 represents 5 tens, which is 10 times as much as 5 ones.) While students can easily see the pattern of adding a 0 at the end of a number when multiplying by 10, they need to be able to justify why this works. • Investigate the pattern, 6, 60, 600, 6,000, 60,000, 600,000 by dividing each number by the previous number.
<p>4.NBT.3. Use place value understanding to round multi-digit whole numbers to any place. ²</p> <p>² Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.</p>	<p>4.NBT.3. When students are asked to round large numbers, they first need to identify which digit is in the appropriate place. Example: Round 76,398 to the nearest 1000.</p> <ul style="list-style-type: none"> • Step 1: Since I need to round to the nearest 1000, then the answer is either 76,000 or 77,000. • Step 2: I know that the halfway point between these two numbers is 76,500. • Step 3: I see that 76,398 is between 76,000 and 76,500. • Step 4: Therefore, the rounded number would be 76,000.

CCSS	Explanations and Examples*
<p>4.NBT.5. Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models. *</p> <p>* Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.</p>	<p>4.NBT.5. Students who develop flexibility in breaking numbers apart have a better understanding of the importance of place value and the distributive property in multi-digit multiplication. Students use base ten blocks, area models, partitioning, compensation strategies, etc. when multiplying whole numbers and use words and diagrams to explain their thinking. They use the terms factor and product when communicating their reasoning. Multiple strategies enable students to develop fluency with multiplication and transfer that understanding to division. Use of the standard algorithm for multiplication is an expectation in the 5th grade.</p> <p>Students may use digital tools to express their ideas.</p> <p>Use of place value and the distributive property are applied in the scaffolded examples below.</p> <ul style="list-style-type: none"> • To illustrate 154×6 students use base 10 blocks or use drawings to show 154 six times. Seeing 154 six times will lead them to understand the distributive property, $154 \times 6 = (100 + 50 + 4) \times 6 = (100 \times 6) + (50 \times 6) + (4 \times 6) = 600 + 300 + 24 = 924$. • The area model shows the partial products. <p>$14 \times 16 = 224$</p> <div data-bbox="1039 1003 1381 1372"> <p>100 4 tens</p> <p>6 tens 24 ones</p> <p>14 16</p> <p>$100 + 40 + 60 + 24 = 224$</p> </div> <p>Using the area model, students first verbalize their understanding:</p> <ul style="list-style-type: none"> • 10×10 is 100 • 4×10 is 40 • 10×6 is 60, and • 4×6 is 24. <p>They used different strategies to record this type of thinking.</p> <p>Continued on next page</p>

CCSS	Explanations and Examples*
	<p>4.NBT.5. Continued</p> <ul style="list-style-type: none">Students explain this strategy and the one below with base 10 blocks, drawings, or numbers.<div><div>25</div><div>× 24</div><div>400 (20 × 20)</div><div>100 (20 × 5)</div><div>80 (4 × 20)</div><div>20 (4 × 5)</div><div>600</div></div><div><div>25</div><div>× 24</div><div>500 (20 × 25)</div><div>100 (4 × 25)</div><div>600</div></div>Matrix model: This model should be introduced after students have facility with the strategies shown above.<div><div><div>20</div><div>5</div></div><div><div>20</div><div>400</div><div>100</div><div>500</div></div><div><div>4</div><div>80</div><div>20</div><div>100</div></div><div><div>600</div></div></div>

CCSS	Explanations and Examples*
<p>4.NBT.6. Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.²</p> <p>² Grade 4 expectations in this domain are limited to whole numbers less than or equal to 1,000,000.</p>	<p>4.NBT.6 In fourth grade, students build on their third grade work with division within 100. Students need opportunities to develop their understandings by using problems in and out of context.</p> <p>Examples:</p> <p>A 4th grade teacher bought 4 new pencil boxes. She has 260 pencils. She wants to put the pencils in the boxes so that each box has the same number of pencils. How many pencils will there be in each box?</p> <ul style="list-style-type: none"> • <u>Using Base 10 Blocks</u>: Students build 260 with base 10 blocks and distribute them into 4 equal groups. Some students may need to trade the 2 hundreds for tens but others may easily recognize that 200 divided by 4 is 50. • <u>Using Place Value</u>: $260 \div 4 = (200 \div 4) + (60 \div 4)$ • <u>Using Multiplication</u>: $4 \times 50 = 200$, $4 \times 10 = 40$, $4 \times 5 = 20$; $50 + 10 + 5 = 65$; so $260 \div 4 = 65$ • <u>Using an Open Array or Area Model</u> After developing an understanding of using arrays to divide, students begin to use a more abstract model for division. This model connects to a recording process that will be formalized in the 5th grade. <p>Example 1: $150 \div 6$ Students make a rectangle and write 6 on one of its sides. They express their understanding that they need to think of the rectangle as representing total of 150.</p> <p>(Student thinking is found on next page)</p> <div data-bbox="1591 1174 1913 1417"> </div>

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CCSS	Explanations and Examples*
	<p>4.NBT.6. Continued [Example 1: $150 \div 6$]</p> <ol style="list-style-type: none"> Students think, 6 times what number is close to 150? They recognize that 6×10 is 60, so they record 10 as a factor and partition the rectangle into 2 rectangles and label the area aligned to the factor of 10 with 60. They express that they have only used 60 of the 150, so they have 90 left. Recognizing that there is another 60 in what is left, they repeat the process above. They express that they have used 120 of the 150, so they have 30 left. Knowing that 6×5 is 30, they write 30 in the bottom area of the rectangle and record 5 as a factor. Students express their calculation in various ways: <ol style="list-style-type: none"> $\begin{array}{r} 150 \\ - 60 \text{ (} 6 \times 10 \text{)} \\ \hline 90 \\ - 60 \text{ (} 6 \times 10 \text{)} \\ \hline 30 \\ - 30 \text{ (} 6 \times 5 \text{)} \\ \hline 0 \end{array}$ $150 \div 6 = 10 + 10 + 5 = 25$ $\begin{array}{rcl} 150 \div 6 & = & (60 \div 6) + (60 \div 6) + (30 \div 6) \\ & = & 10 + 10 + 5 = 25 \end{array}$ <p>Example 2: $1917 \div 9$</p> <p>A student's description of his or her thinking may be: I need to find out how many 9s are in 1917. I know that 200×9 is 1800. So if I use 1800 of the 1917, I have 117 left. I know that 9×10 is 90. So if I have 10 more 9s, I will have 27 left. I can make 3 more 9s. I have 200 nines, 10 nines and 3 nines. So I made 213 nines. $1917 \div 9 = 213$.</p> <p>Students may use digital tools to express ideas.</p> 

Concepts What Students Need to Know	Skills What Students Need To Be Able To Do	Required and Suggested Activities
Multi-digit whole numbers	<p>READ (using base-ten numerals, number names and expanded form)</p> <p>WRITE (using base-ten numerals, number names and expanded form)</p> <p>COMPARE (two multi-digit numbers based on digits in each place using $>$, $=$, $<$ symbols)</p> <p>ROUND (to any place using place value understanding)</p> <p>MULTIPLY (using strategies based on place value and properties of operations)</p> <ul style="list-style-type: none"> (up to four-digit by one-digit) (two-digit by two-digit) <p>ILLUSTRATE (calculation using equations, rectangular arrays and/or area models)</p> <p>EXPLAIN (calculation using equations, rectangular arrays and/or area models)</p>	<ul style="list-style-type: none"> Required: <ul style="list-style-type: none"> Grade 4 Pre Test Daily Warm up sheets (# for the day it is) Related MCAS Questions (can be used as assessments) Suggested: <ul style="list-style-type: none"> Trailblazers <ul style="list-style-type: none"> Unit _____ Lesson _____ Unit _____ Lesson _____ Unit _____ Lesson _____ Unit _____ Lesson _____ Unit _____ Lesson _____ Unit _____ Lesson _____
Digit	<p>RECOGNIZE (a digit in the ones place represents 10 times what it represents in the place to its right)</p>	OnCore Assessments and Lessons
Whole number quotients and remainders	<p>FIND (up to four-digit dividend and one-digit divisors using strategies based on place value, properties of operations, and/or relationships between multiplication and division)</p> <p>ILLUSTRATE (calculation using equations, rectangular arrays and/or area models)</p> <p>EXPLAIN (calculation using equations, rectangular arrays and/or area models)</p>	

Unit Assessments

The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 2 - Factors and Multiples

Pacing: 2 weeks

Mathematical Practices
<p><i>Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.</i></p> <p><i>Practices in bold are to be emphasized in the unit.</i></p> <ol style="list-style-type: none">1. Make sense of problems and persevere in solving them.2. Reason abstractly and quantitatively.3. Construct viable arguments and critique the reasoning of others.4. Model with mathematics.5. Use appropriate tools strategically.6. Attend to precision.7. Look for and make use of structure.8. Look for and express regularity in repeated reasoning.
Domain and Standards Overview
<p>Operations and Algebraic Thinking</p> <ul style="list-style-type: none">• Use the four operations with whole numbers to solve problems.• Gain familiarity with factors and multiples.• Generate and analyze patterns.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 2 - Factors and Multiples

CCSS	Explanations and Examples*
<p>4.OA.4. Find all factor pairs for a whole number in the range 1–100. Recognize that a whole number is a multiple of each of its factors. Determine whether a given whole number in the range 1–100 is a multiple of a given one-digit number. Determine whether a given whole number in the range 1–100 is prime or composite.</p>	<p>4.OA.4. Students should understand the process of finding factor pairs so they can do this for any number 1 -100, not just those within the basic multiplication facts.</p> <p>Example: Factor pairs for 96: 1 and 96, 2 and 48, 3 and 32, 4 and 24, 6 and 16, 8 and 12.</p> <p>Multiples can be thought of as the result of skip counting by each of the factors. When skip counting, students should be able to identify the number of factors counted e.g., 5, 10, 15, 20 (there are 4 fives in 20).</p> <p>Example: Factors of 24: 1, 2, 3, 4, 6, 8, 12, 24 Multiples : 1, 2, 3, 4, 5...24 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24 3, 6, 9, 12, 15, 18, 21, 24 4, 8, 12, 16, 20, 24 8, 16, 24 12, 24 24</p> <p>To determine if a number between 1-100 is a multiple of a given one-digit number, some helpful hints include the following:</p> <ul style="list-style-type: none"> • all even numbers are multiples of 2 • all even numbers that can be halved twice (with a whole number result) are multiples of 4 • all numbers ending in 0 or 5 are multiples of 5 <p>Continued on next page</p>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 2 - Factors and Multiples

CCSS	Explanations and Examples*
	<p>4.OA.4. Continued</p> <p>Prime vs. Composite: A prime number is a number greater than 1 that has only 2 factors, 1 and itself. Composite numbers have more than 2 factors.</p> <p>Students investigate whether numbers are prime or composite by</p> <ul style="list-style-type: none"> • building rectangles (arrays) with the given area and finding which numbers have more than two rectangles (e.g. 7 can be made into only 2 rectangles, 1 x 7 and 7 x 1, therefore it is a prime number) • finding factors of the number
<p>4.OA.1. Interpret a multiplication equation as a comparison, e.g., interpret $35 = 5 \times 7$ as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.</p>	<p>4.OA.1. A <i>multiplicative comparison</i> is a situation in which one quantity is multiplied by a specified number to get another quantity (e.g., “<i>a</i> is <i>n</i> times as much as <i>b</i>”). Students should be able to identify and verbalize which quantity is being multiplied and which number tells how many times.</p>
<p>4.OA.5. Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. <i>For example, given the rule “Add 3” and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.</i></p>	<p>4.OA.5. Patterns involving numbers or symbols either repeat or grow. Students need multiple opportunities creating and extending number and shape patterns. Numerical patterns allow students to reinforce facts and develop fluency with operations.</p> <p>Patterns and rules are related. A pattern is a sequence that repeats the same process over and over. A rule dictates what that process will look like. Students investigate different patterns to find rules, identify features in the patterns, and justify the reason for those features.</p> <p>Continued on next page</p>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 2 - Factors and Multiples

CCSS	Explanations and Examples*									
	<p>4.OA.5. Continued</p> <p>Examples:</p> <table><tr><th>Pattern</th><th>Rule</th><th>Feature(s)</th></tr><tr><td>3, 8, 13, 18, 23, 28, ...</td><td>Start with 3, add 5</td><td>The numbers alternately end with a 3 or 8</td></tr><tr><td>5, 10, 15, 20...</td><td>Start with 5, add 5</td><td>The numbers are multiples of 5 and end with either 0 or 5. The numbers that end with 5 are products of 5 and an odd number. The numbers that end in 0 are products of 5 and an even number.</td></tr></table> <p>After students have identified rules and features from patterns, they need to generate a numerical or shape pattern from a given rule.</p> <p>Example:</p> <p>Rule: Starting at 1, create a pattern that starts at 1 and multiplies each number by 3. Stop when you have 6 numbers.</p> <p>Students write 1, 3, 9, 27, 81, 243. Students notice that all the numbers are odd and that the sums of the digits of the 2 digit numbers are each 9. Some students might investigate this beyond 6 numbers. Another feature to investigate is the patterns in the differences of the numbers (3 - 1 = 2, 9 - 3 = 6, 27 - 9 = 18, etc.)</p>	Pattern	Rule	Feature(s)	3, 8, 13, 18, 23, 28, ...	Start with 3, add 5	The numbers alternately end with a 3 or 8	5, 10, 15, 20...	Start with 5, add 5	The numbers are multiples of 5 and end with either 0 or 5. The numbers that end with 5 are products of 5 and an odd number. The numbers that end in 0 are products of 5 and an even number.
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Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 2 - Factors and Multiples

Concepts What Students Need to Know	Skills What Students Need To Be Able To Do	<u>Required</u> and Suggested Activities
<p>Factor Pairs</p> <p>Whole Number</p> <p>Multiplicative Equations</p> <p>Multiplicative Comparisons</p> <p>Pattern</p>	<p>FIND (for a whole number 1-100)</p> <p>RECOGNIZE (that it's a multiple of each of its factors)</p> <p>DETERMINE</p> <ul style="list-style-type: none"> • (if it's a multiple of a given one-digit number) • (whether prime or composite) <p>INTERPRET (as multiplicative comparisons)</p> <p>REPRESENT (as verbal statements of multiplicative equations)</p> <p>GENERATE (number or shape that follows a given rule)</p> <p>IDENTIFY (features not explicit in rule itself)</p>	<ul style="list-style-type: none"> • Required: <ul style="list-style-type: none"> ○ Daily Warm up sheets (# for the day it is) ○ Related MCAS Questions (can be used as assessments) • Suggested: <ul style="list-style-type: none"> ○ Trailblazers <ul style="list-style-type: none"> ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ <p>OnCore Assessments and Lessons</p>

Unit Assessments
The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 3- Multi-Digit Whole Number Computation

Pacing: 3 weeks

Mathematical Practices
<p><i>Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.</i></p> <p><i>Practices in bold are to be emphasized in the unit.</i></p> <ol style="list-style-type: none">1. Make sense of problems and persevere in solving them.2. Reason abstractly and quantitatively.3. Construct viable arguments and critique the reasoning of others.4. Model with mathematics.5. Use appropriate tools strategically.6. Attend to precision.7. Look for and make use of structure.8. Look for and express regularity in repeated reasoning.

Domain and Standards Overview
<p>Operations and Algebraic Thinking</p> <ul style="list-style-type: none">• Use the four operations with whole numbers to solve problems. <p>Number and Operations in Base Ten</p> <ul style="list-style-type: none">• Use place value understanding and properties of operations to perform multi-digit arithmetic.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 3- Multi-Digit Whole Number Computation

CCSS	Explanations and Examples*
<p>4.OA.3. Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.</p>	<p>4.OA.3. Students need many opportunities solving multistep story problems using all four operations.</p> <p>An interactive whiteboard, document camera, drawings, words, numbers, and/or objects may be used to help solve story problems.</p> <p>Example:</p> <p>Chris bought clothes for school. She bought 3 shirts for \$12 each and a skirt for \$15. How much money did Chris spend on her new school clothes?</p> $3 \times \$12 + \$15 = a$ <p>In division problems, the remainder is the whole number left over when as large a multiple of the divisor as possible has been subtracted.</p> <p>Example:</p> <p>Kim is making candy bags. There will be 5 pieces of candy in each bag. She had 53 pieces of candy. She ate 14 pieces of candy. How many candy bags can Kim make now? (7 bags with 4 leftover)</p> <p>Kim has 28 cookies. She wants to share them equally between herself and 3 friends. How many cookies will each person get? (7 cookies each) $28 \div 4 = a$</p> <p>There are 29 students in one class and 28 students in another class going on a field trip. Each car can hold 5 students. How many cars are needed to get all the students to the field trip? (12 cars, one possible explanation is 11 cars holding 5 students and the 12th holding the remaining 2 students)</p> $29 + 28 = 11 \times 5 + 2$ <p>Continued on next page</p>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 3- Multi-Digit Whole Number Computation

CCSS	Explanations and Examples*
	<p>4.OA.3. Continued</p> <p>Estimation skills include identifying when estimation is appropriate, determining the level of accuracy needed, selecting the appropriate method of estimation, and verifying solutions or determining the reasonableness of situations using various estimation strategies.</p> <p>Estimation strategies include, but are not limited to:</p> <ul style="list-style-type: none"> • front-end estimation with adjusting (using the highest place value and estimating from the front end, making adjustments to the estimate by taking into account the remaining amounts), • clustering around an average (when the values are close together an average value is selected and multiplied by the number of values to determine an estimate), • rounding and adjusting (students round down or round up and then adjust their estimate depending on how much the rounding affected the original values), • using friendly or compatible numbers such as factors (students seek to fit numbers together - e.g., rounding to factors and grouping numbers together that have round sums like 100 or 1000), • using benchmark numbers that are easy to compute (students select close whole numbers for fractions or decimals to determine an estimate).
<p>4.NBT.4. Fluently add and subtract multi-digit whole numbers using the standard algorithm.</p>	<p>4.NBT.4. Students build on their understanding of addition and subtraction, their use of place value and their flexibility with multiple strategies to make sense of the standard algorithm. They continue to use place value in describing and justifying the processes they use to add and subtract.</p> <p>When students begin using the standard algorithm their explanation may be quite lengthy. After much practice with using place value to justify their steps, they will develop fluency with the algorithm. Students should be able to explain why</p>

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CCSS	Explanations and Examples*
	<p>the algorithm works.</p> $\begin{array}{r} 3892 \\ + 1567 \\ \hline \end{array}$ <p>Student explanation for this problem:</p> <ol style="list-style-type: none"> 1. Two ones plus seven ones is nine ones. 2. Nine tens plus six tens is 15 tens. 3. I am going to write down five tens and think of the 10 tens as one more hundred. (notates with a 1 above the hundreds column) 4. Eight hundreds plus five hundreds plus the extra hundred from adding the tens is 14 hundreds. 5. I am going to write the four hundreds and think of the 10 hundreds as one more 1000. (notates with a 1 above the thousands column) 6. Three thousands plus one thousand plus the extra thousand from the hundreds is five thousand. $\begin{array}{r} 3546 \\ - 928 \\ \hline \end{array}$ <p>Student explanation for this problem is on next page:</p> <p>Continued on next page</p> <p>4.NBT.4. Continued</p> <ol style="list-style-type: none"> 1. There are not enough ones to take 8 ones from 6 ones so I have to use one ten as 10 ones. Now I have 3 tens and 16 ones. (Marks through the 4 and notates with a 3 above the 4 and writes a 1 above the ones column to be represented as 16 ones.) 2. Sixteen ones minus 8 ones is 8 ones. (Writes an 8 in the ones column of answer.)

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Unit 3- Multi-Digit Whole Number Computation

CCSS	Explanations and Examples*						
	<div>3. Three tens minus 2 tens is one ten. (Writes a 1 in the tens column of answer.)</div> <div>4. There are not enough hundreds to take 9 hundreds from 5 hundreds so I have to use one thousand as 10 hundreds. (Marks through the 3 and notates with a 2 above it. (Writes down a 1 above the hundreds column.) Now I have 2 thousand and 15 hundreds.</div> <div>5. Fifteen hundreds minus 9 hundreds is 6 hundreds. (Writes a 6 in the hundreds column of the answer).</div> <div>6. I have 2 thousands left since I did not have to take away any thousands. (Writes 2 in the thousands place of answer.)</div> <div>Note: Students should know that it is mathematically possible to subtract a larger number from a smaller number but that their work with whole numbers does not allow this as the difference would result in a negative number.</div>						
<div>4.OA.2. Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.¹</div> <div>¹ See Glossary, Table 2</div>	<div>4.OA.2. Students need many opportunities to solve contextual problems.</div> <div>Table 2 in the glossary included the following multiplication problem:</div> <div>“A blue hat costs \$6. A red hat costs 3 times as much as the blue hat. How much does the red hat cost?”</div> <div>Continued on next page</div> <div>4.OA.2. Continued In solving this problem, the student should identify \$6 as the quantity that is being multiplied by 3. The student should write the problem using a symbol to represent the unknown.</div> <div>(\$6 × 3 = □)</div> <div><div>red hat</div><table><tr><td colspan="3">\$18</td></tr></table></div> <div><div>blue hat</div><table><tr><td>\$6</td><td>\$6</td><td>\$6</td></tr></table></div>	\$18			\$6	\$6	\$6
\$18							
\$6	\$6	\$6					

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 3- Multi-Digit Whole Number Computation

CCSS	Explanations and Examples*						
	<div>3</div> <p>Table 2 in the glossary includes the following division problem:</p> <p>A red hat costs \$18 and a blue hat costs \$6. How many times as much does the red hat cost as the blue hat?</p> <p>In solving this problem, the student should identify \$18 as the quantity being divided into shares of \$6. The student should write the problem using a symbol to represent the unknown.</p> <p>(\$18 ÷ \$6 = □)</p> <div><div>blue hat</div><div>\$6</div><div>red hat</div><div><table><tr><td>\$6</td><td>\$6</td><td>\$6</td></tr><tr><td colspan="3">\$18</td></tr></table></div></div> <p>When distinguishing multiplicative comparison from additive comparison, students should note that</p> <ul style="list-style-type: none">• additive comparisons focus on the difference between two quantities (e.g., Deb has 3 apples and Karen has 5 apples. How many more apples does Karen have?). A simple way to remember this is, “How many more?” <p>Continued on next page</p> <p>4.OA.2. Continued</p> <ul style="list-style-type: none">• multiplicative comparisons focus on comparing two quantities by showing that one quantity is a specified number of times larger or smaller than the other (e.g., Deb ran 3 miles. Karen ran 5 times as many miles as Deb. How many miles did Karen run?). A simple way to remember this is “How many times as much?” or “How many times as many?”	\$6	\$6	\$6	\$18		
\$6	\$6	\$6					
\$18							

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 3- Multi-Digit Whole Number Computation

Concepts What Students Need to Know	Skills What Students Need To Be Able To Do	<u>Required</u> and Suggested Activities
<p>Multi-step Word Problems</p> <p>Reasonableness of Answers</p> <p>Multi-digit Whole Numbers</p>	<p>SOLVE (whole numbers with whole-number answers using four operations) REPRESENT (using equations with letter for unknown quantity) MULTIPLY (involving multiplicative comparison) DIVIDE (involving multiplicative comparison)</p> <p>ASSESS (using mental computation and estimation strategies including rounding)</p> <p>ADD (fluently using standard algorithm) SUBTRACT (fluently using standard algorithm)</p>	<ul style="list-style-type: none"> • Required: <ul style="list-style-type: none"> Daily Warm up sheets (# for the day it is) ○ Related MCAS Questions (can be used as assessments) • Suggested: <ul style="list-style-type: none"> ○ Trailblazers <ul style="list-style-type: none"> ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ <p>OnCore Assessments and Lessons</p>

Unit Assessments The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 4- Comparing Fractions and Understanding Decimal Notation

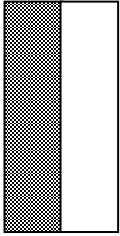
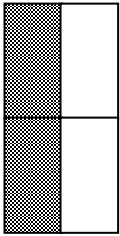
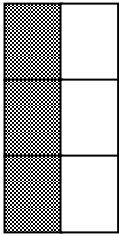
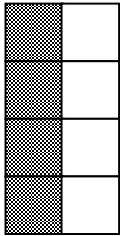
Pacing: 4 weeks

Mathematical Practices
<p><i>Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.</i></p> <p><i>Practices in bold are to be emphasized in the unit.</i></p> <ol style="list-style-type: none">1. Make sense of problems and persevere in solving them.2. Reason abstractly and quantitatively.3. Construct viable arguments and critique the reasoning of others.4. Model with mathematics.5. Use appropriate tools strategically.6. Attend to precision.7. Look for and make use of structure.8. Look for and express regularity in repeated reasoning.
Domain and Standards Overview
<p>Number and Operations—Fractions</p> <ul style="list-style-type: none">• Extend understanding of fraction equivalence and ordering.• Understand decimal notation for fractions, and compare decimal fractions.

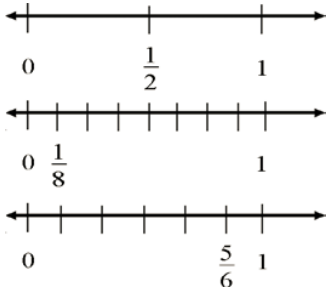
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Grade 4 Mathematics

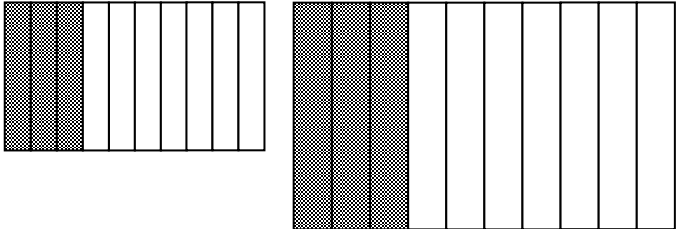
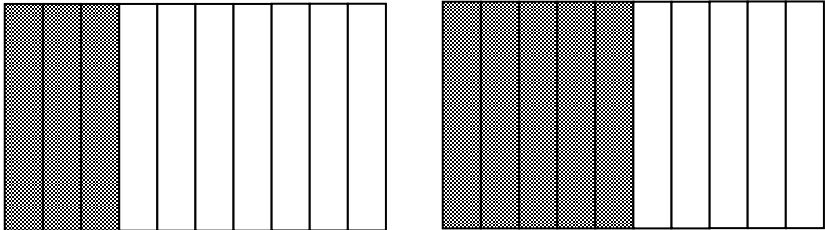
Unit 4- Comparing Fractions and Understanding Decimal Notation

CCSS	Explanations and Examples*
<p>4.NF.1. Explain why a fraction a/b is equivalent to a fraction $(n \times a)/(n \times b)$ by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions</p>	<p>4.NF.1. This standard extends the work in third grade by using additional denominators (5, 10, 12, and 100). [Grade 3 expectations are limited to fractions with denominators of 2, 3, 4, 6, and 8.]</p> <p>Students can use visual models or applets to generate equivalent fractions.</p> <p>All the models show $1/2$. The second model shows $2/4$ but also shows that $1/2$ and $2/4$ are equivalent fractions because their areas are equivalent. When a horizontal line is drawn through the center of the model, the number of equal parts doubles and size of the parts is halved.</p> <p>Students will begin to notice connections between the models and fractions in the way both the parts and wholes are counted and begin to generate a rule for writing equivalent fractions.</p> <p>$1/2 \times 2/2 = 2/4$.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>$\frac{1}{2}$</p> </div> <div style="text-align: center;">  <p>$\frac{2}{4} = \frac{2 \times 1}{2 \times 2}$</p> </div> <div style="text-align: center;">  <p>$\frac{3}{6} = \frac{3 \times 1}{3 \times 2}$</p> </div> <div style="text-align: center;">  <p>$\frac{4}{8} = \frac{4 \times 1}{4 \times 2}$</p> </div> </div> <p>Technology Connection: http://illuminations.nctm.org/activitydetail.aspx?id=80</p>

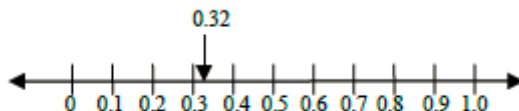
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Grade 4 Mathematics
Unit 4- Comparing Fractions and Understanding Decimal Notation

CCSS	Explanations and Examples*
<p>4.NF.2. Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators or by comparing to a benchmark fraction such as $\frac{1}{2}$. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.</p>	<p>4.NF.2. Benchmark fractions include common fractions between 0 and 1 such as halves, thirds, fourths, fifths, sixths, eighths, tenths, twelfths, and hundredths.</p> <p>Fractions can be compared using benchmarks, common denominators, or common numerators. Symbols used to describe comparisons include $<$, $>$, $=$.</p> <p>Fractions may be compared using $\frac{1}{2}$ as a benchmark.</p>  <p>Possible student thinking by using benchmarks: $\frac{1}{8}$ is smaller than $\frac{1}{2}$ because when 1 whole is cut into pieces, the pieces are much smaller than when 1 whole is cut into 2 pieces.</p> <p>Possible student thinking by creating common denominators:</p> $\frac{5}{6} > \frac{1}{2} \text{ because } \frac{3}{6} = \frac{1}{2} \text{ and } \frac{5}{6} > \frac{3}{6}$ <p>Fractions with common denominators may be compared using the numerators as a guide: $\frac{2}{6} < \frac{3}{6} < \frac{5}{6}$</p> <p>Fractions with common numerators may be compared and ordered using the denominators as a guide: $\frac{3}{10} < \frac{3}{8} < \frac{3}{4}$</p>

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Grade 4 Mathematics
Unit 4- Comparing Fractions and Understanding Decimal Notation

CCSS	Explanations and Examples*
<p>4.NF.7. Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual model.</p>	<p>4.NF.7 Students build area and other models to compare decimals. Through these experiences and their work with fraction models, they build the understanding that comparisons between decimals or fractions are only valid when the whole is the same for both cases. Each of the models below shows $\frac{3}{10}$ but the whole on the right is much bigger than the whole on the left. They are both $\frac{3}{10}$ but the model on the right is a much larger quantity than the model on the left.</p> <div style="text-align: center;">  </div> <p>When the wholes are the same, the decimals or fractions can be compared.</p> <p>Example:</p> <ul style="list-style-type: none"> • Draw a model to show that $0.3 < 0.5$. (Students would sketch two models of approximately the same size to show the area that represents three-tenths is smaller than the area that represents five-tenths. <div style="text-align: center;">  </div>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 4- Comparing Fractions and Understanding Decimal Notation

CCSS	Explanations and Examples*												
<p>4.NF.5. Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100.⁴ <i>For example, express 3/10 as 30/100, and add 3/10 + 4/100 = 34/100.</i></p> <p>⁴ Students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators in general; but addition and subtraction with unlike denominators in general is not a requirement of this grade.</p>	<p>4.NF.5. Students can use base ten blocks, graph paper, and other place value models to explore the relationship between fractions with denominators of 10 and denominators of 100.</p> <p>Students may represent 3/10 with 3 longs and may also write the fraction as 30/100 with the whole in this case being the flat (the flat represents one hundred units with each unit equal to one hundredth). Students begin to make connections to the place value chart as shown in 4.NF.6.</p> <p>This work in fourth grade lays the foundation for performing operations with decimal numbers in fifth grade.</p>												
<p>4.NF.6. Use decimal notation for fractions with denominators 10 or 100. <i>For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram.</i></p>	<p>4.NF.6. Students make connections between fractions with denominators of 10 and 100 and the place value chart. By reading fraction names, students say 32/100 as thirty-two hundredths and rewrite this as 0.32 or represent it on a place value model as shown below.</p> <table><tr><td>Hundreds</td><td>Tens</td><td>Ones</td><td>●</td><td>Tenths</td><td>Hundredths</td></tr><tr><td></td><td></td><td></td><td>●</td><td>3</td><td>2</td></tr></table> <p>Students use the representations explored in 4.NF.5 to understand 32/100 can be expanded to 3/10 and 2/100.</p> <p>Students represent values such as 0.32 or 32/100 on a number line. 32/100 is more than 30/100 (or 3/10) and less than 40/100 (or 4/10). It is closer to 30/100 so it would be placed on the number line near that value.</p> 	Hundreds	Tens	Ones	●	Tenths	Hundredths				●	3	2
Hundreds	Tens	Ones	●	Tenths	Hundredths								
			●	3	2								

Grade 4 Mathematics
Unit 4- Comparing Fractions and Understanding Decimal Notation

Grade 4 Mathematics

Unit 4- Comparing Fractions and Understanding Decimal Notation

<p align="center">Unit Assessments</p> <p>The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.</p>	
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Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 5- Building Understanding of Addition, Subtraction and Multiplication of Fractions

Pacing: 6 weeks

Mathematical Practices
<p><i>Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.</i></p> <p><i>Practices in bold are to be emphasized in the unit.</i></p> <ol style="list-style-type: none">1. Make sense of problems and persevere in solving them.2. Reason abstractly and quantitatively.3. Construct viable arguments and critique the reasoning of others.4. Model with mathematics.5. Use appropriate tools strategically.6. Attend to precision.7. Look for and make use of structure.8. Look for and express regularity in repeated reasoning
Domain and Standards Overview
<p>Number and Operations—Fractions</p> <ul style="list-style-type: none">• Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers.

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Grade 4 Mathematics

Unit 5- Building Understanding of Addition, Subtraction and Multiplication of Fractions

CCSS	Explanations and Examples*
<p>4.NF.3. Understand a fraction a/b with $a > 1$ as a sum of fractions $1/b$.³</p> <ul style="list-style-type: none"> a. Understand addition and subtraction of fractions as joining and separating parts referring to the same whole. b. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. <i>Examples: $3/8 = 1/8 + 1/8 + 1/8$; $3/8 = 1/8 + 2/8$; $2\ 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8$.</i> c. Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction. d. Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem. <p>³ Grade 4 expectations in this domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100.</p>	<p>4.NF.3. A fraction with a numerator of one is called a unit fraction. When students investigate fractions other than unit fractions, such as $2/3$, they should be able to decompose the non-unit fraction into a combination of several unit fractions.</p> <p>Example: $2/3 = 1/3 + 1/3$</p> <p>Being able to visualize this decomposition into unit fractions helps students when adding or subtracting fractions. Students need multiple opportunities to work with mixed numbers and be able to decompose them in more than one way. Students may use visual models to help develop this understanding.</p> <p>Example: $1\frac{1}{4} - \frac{3}{4} = \square$</p> $\frac{4}{4} + \frac{1}{4} = \frac{5}{4}$ $\frac{5}{4} - \frac{3}{4} = \frac{2}{4} \text{ or } \frac{1}{2}$ <p>Example of word problem:</p> <ul style="list-style-type: none"> • Mary and Lacey decide to share a pizza. Mary ate $3/6$ and Lacey ate $2/6$ of the pizza. How much of the pizza did the girls eat together? <p>Solution: The amount of pizza Mary ate can be thought of a $3/6$ or $1/6$ and $1/6$ and $1/6$. The amount of pizza Lacey ate can be thought of a $1/6$ and $1/6$. The total amount of pizza they ate is $1/6 + 1/6 + 1/6 + 1/6 + 1/6$ or $5/6$ of the whole pizza.</p> <p>Continued on next page</p> <p>4.NF.3. Continued</p> <p>A separate algorithm for mixed numbers in addition and subtraction is not necessary. Students will tend to add or subtract the whole numbers first and then work with the fractions using the same strategies they have applied to</p>

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Grade 4 Mathematics

Unit 5- Building Understanding of Addition, Subtraction and Multiplication of Fractions

problems that contained only fractions.

Example:

- Susan and Maria need $8\frac{3}{8}$ feet of ribbon to package gift baskets. Susan has $3\frac{1}{8}$ feet of ribbon and Maria has $5\frac{3}{8}$ feet of ribbon. How much ribbon do they have altogether? Will it be enough to complete the project? Explain why or why not.

The student thinks: I can add the ribbon Susan has to the ribbon Maria has to find out how much ribbon they have altogether. Susan has $3\frac{1}{8}$ feet of ribbon and Maria has $5\frac{3}{8}$ feet of ribbon. I can write this as $3\frac{1}{8} + 5\frac{3}{8}$. I know they have 8 feet of ribbon by adding the 3 and 5. They also have $\frac{1}{8}$ and $\frac{3}{8}$ which makes a total of $\frac{4}{8}$ more. Altogether they have $8\frac{4}{8}$ feet of ribbon. $8\frac{4}{8}$ is larger than $8\frac{3}{8}$ so they will have enough ribbon to complete the project. They will even have a little extra ribbon left, $\frac{1}{8}$ foot.

Example:

- Trevor has $4\frac{1}{8}$ pizzas left over from his soccer party. After giving some pizza to his friend, he has $2\frac{4}{8}$ of a pizza left. How much pizza did Trevor give to his friend?

Solution: Trevor had $4\frac{1}{8}$ pizzas to start. This is $\frac{33}{8}$ of a pizza. The x's show the pizza he has left which is $2\frac{4}{8}$ pizzas or $\frac{20}{8}$ pizzas. The shaded rectangles without the x's are the pizza he gave to his friend which is $\frac{13}{8}$ or $1\frac{5}{8}$ pizzas.



Wilmington Curriculum Design Unit Planner and Pacing Guide

Grade 4 Mathematics

Unit 5- Building Understanding of Addition, Subtraction and Multiplication of Fractions

4.NF.4. Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.³

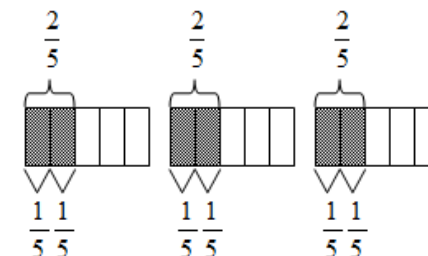
- Understand a fraction a/b as a multiple of $1/b$. For example, use a visual fraction model to represent $5/4$ as the product $5 \times (1/4)$, recording the conclusion by the equation $5/4 = 5 \times (1/4)$.
- Understand a multiple of a/b as a multiple of $1/b$, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as $6/5$. (In general, $n \times (a/b) = (n \times a)/b$.)
- Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. For example, if each person at a party will eat $3/8$ of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?

³ Grade 4 expectations in this domain are limited to fractions with denominators 2, 3, 4, 5, 6, 8, 10, 12, and 100.

4.NF.4. Students need many opportunities to work with problems in context to understand the connections between models and corresponding equations. Contexts involving a whole number times a fraction lend themselves to modeling and examining patterns.

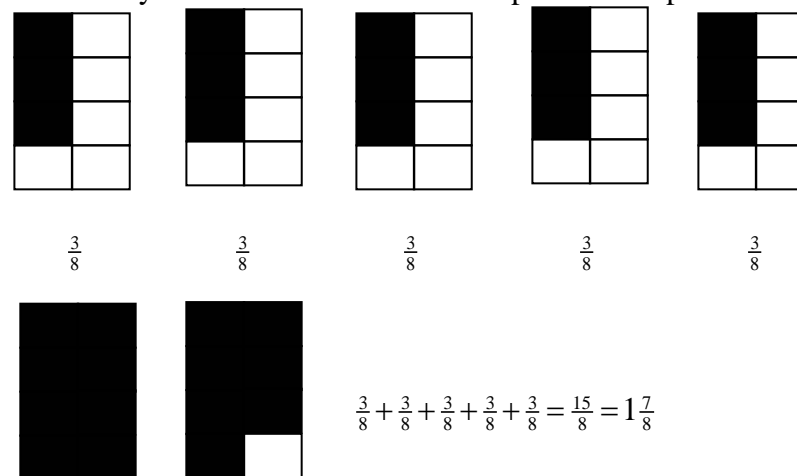
Examples:

- $3 \times (2/5) = 6 \times (1/5) = 6/5$



- If each person at a party eats $3/8$ of a pound of roast beef, and there are 5 people at the party, how many pounds of roast beef are needed? Between what two whole numbers does your answer lie?

A student may build a fraction model to represent this problem:



Wilmington Curriculum Design Unit Planner and Pacing Guide

Grade 4 Mathematics

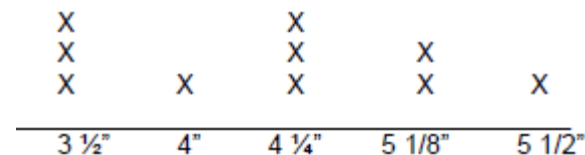
Unit 5- Building Understanding of Addition, Subtraction and Multiplication of Fractions

4.MD.4. Make a line plot to display a data set of measurements in fractions of a unit ($\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$). Solve problems involving addition and subtraction of fractions by using information presented in line plots. *For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection.*

4.MD.4.

Example:

Ten students in Room 31 measured their pencils at the end of the day. They recorded their results on the line plot below.



Possible questions:

- What is the difference in length from the longest to the shortest pencil?
- If you were to line up all the pencils, what would the total length be?
- If the $5\frac{1}{8}"$ pencils are placed end to end, what would be their total length

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 5- Building Understanding of Addition, Subtraction and Multiplication of Fractions

Concepts What Students Need to Know	Skills What Students Need To Be Able To Do	Required and Suggested Activities
Addition of Fractions	UNDERSTAND (as joining parts referring to the same whole) SOLVE (word problems with like denominators) SOLVE (problems using information from line plots)	<ul style="list-style-type: none"> • Required: Daily Warm up sheets (# for the day it is) <ul style="list-style-type: none"> ○ Related MCAS Questions (can be used as assessments) • Suggested: <ul style="list-style-type: none"> ○ Trailblazers <ul style="list-style-type: none"> ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ <p>OnCore Assessments and Lessons</p>
Subtraction of Fractions	UNDERSTAND (as separating parts referring to the same whole) SOLVE (word problems with like denominators) SOLVE (problems using information from line plots)	
Decomposition of Fractions	RECORD (into a sum of fractions with same denominator in more than one way using an equation) JUSTIFY (using a visual fraction model)	
Mixed Numbers	ADD (with like denominators by replacing with equivalent fractions and/or properties of operations) SUBTRACT (with like denominators by replacing with equivalent fractions and/or properties of operations)	
Multiplication of Fractions	MULTIPLY (by a whole number) UNDERSTAND (a fraction a/b as a multiple of $1/b$) UNDERSTAND (a multiple of a/b as a multiple of $1/b$) SOLVE (word problems by a whole number)	
Line Plots	MAKE (to display data involving fractions)	

Unit Assessments

The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 6 - Solving Problems involving Measurement and Data

Pacing: 3 weeks

Mathematical Practices
<p><i>Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.</i></p> <p><i>Practices in bold are to be emphasized in the unit.</i></p> <ol style="list-style-type: none">1. Make sense of problems and persevere in solving them.2. Reason abstractly and quantitatively.3. Construct viable arguments and critique the reasoning of others.4. Model with mathematics.5. Use appropriate tools strategically.6. Attend to precision.7. Look for and make use of structure.8. Look for and express regularity in repeated reasoning.
Domain and Standards Overview
<p>Measurement and Data</p> <ul style="list-style-type: none">• Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit.• Represent and interpret data.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 6 - Solving Problems involving Measurement and Data

CCSS	Explanations and Examples*																																
<p>4.MD.1. Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a two-column table. For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36), ... *</p> <p>* It is the belief of the design team that this standard should also be included in <i>Unit 4: Comparing Fractions and Understanding Decimal Notation</i> so that students have opportunities to connect and apply understanding of decimals to the metric system.</p>	<p>4.MD.1. The units of measure that have not been addressed in prior years are pounds, ounces, kilometers, milliliters, and seconds. Students’ prior experiences were limited to measuring length, mass, liquid volume, and elapsed time. Students did not convert measurements. Students need ample opportunities to become familiar with these new units of measure.</p> <p>Students may use a two-column chart to convert from larger to smaller units and record equivalent measurements. They make statements such as, if one foot is 12 inches, then 3 feet has to be 36 inches because there are 3 groups of 12.</p> <p>Example:</p> <table><tr><td>kg</td><td>g</td><td></td><td>ft</td><td>in</td><td></td><td>lb</td><td>oz</td></tr><tr><td>1</td><td>1000</td><td></td><td>1</td><td>12</td><td></td><td>1</td><td>16</td></tr><tr><td>2</td><td>2000</td><td></td><td>2</td><td>24</td><td></td><td>2</td><td>32</td></tr><tr><td>3</td><td>3000</td><td></td><td>3</td><td>36</td><td></td><td>3</td><td>48</td></tr></table>	kg	g		ft	in		lb	oz	1	1000		1	12		1	16	2	2000		2	24		2	32	3	3000		3	36		3	48
kg	g		ft	in		lb	oz																										
1	1000		1	12		1	16																										
2	2000		2	24		2	32																										
3	3000		3	36		3	48																										
<p>4.MD.2. Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.</p>	<p>4.MD.2. Examples:</p> <p><u>Division/fractions</u>: Susan has 2 feet of ribbon. She wants to give her ribbon to her 3 best friends so each friend gets the same amount. How much ribbon will each friend get?</p> <p>Students may record their solutions using fractions or inches. (The answer would be 2/3 of a foot or 8 inches. Students are able to express the answer in inches because they understand that 1/3 of a foot is 4 inches and 2/3 of a foot is 2 groups of 1/3.)</p> <p>Continued on next page</p> <p>4.MD.2. Continued</p> <p><u>Addition</u>: Mason ran for an hour and 15 minutes on Monday, 25 minutes on Tuesday, and 40 minutes on Wednesday. What was the total number of minutes</p>																																

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 6 - Solving Problems involving Measurement and Data

CCSS	Explanations and Examples*
	<p>Mason ran?</p> <p><u>Subtraction</u>: A pound of apples costs \$1.20. Rachel bought a pound and a half of apples. If she gave the clerk a \$5.00 bill, how much change will she get back?</p> <p><u>Multiplication</u>: Mario and his 2 brothers are selling lemonade. Mario brought one and a half liters, Javier brought 2 liters, and Ernesto brought 450 milliliters. How many total milliliters of lemonade did the boys have?</p> <p>Number line diagrams that feature a measurement scale can represent measurement quantities. Examples include: ruler, diagram marking off distance along a road with cities at various points, a timetable showing hours throughout the day, or a volume measure on the side of a container.</p>
<p>4.MD.3. Apply the area and perimeter formulas for rectangles in real world and mathematical problems. <i>For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor.</i></p>	<p>4.MD.3. Students developed understanding of area and perimeter in 3rd grade by using visual models.</p> <p>While students are expected to use formulas to calculate area and perimeter of rectangles, they need to understand and be able to communicate their understanding of why the formulas work.</p> <p>The formula for area is $l \times w$ and the answer will always be in square units.</p> <p>The formula for perimeter can be $2l + 2w$ or $2(l + w)$ and the answer will be in linear units.</p>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 6 - Solving Problems involving Measurement and Data

Concepts What Students Need to Know	Skills What Students Need To Be Able To Do	<u>Required</u> and Suggested Activities
<p>Measurement Units</p> <p>Types of Measure</p> <ul style="list-style-type: none"> • Distance • Time • Volume • Mass • Money <p>Rectangles</p>	<p>KNOW (relative sizes within one system of units)</p> <p>EXPRESS (measurements in a larger unit in terms of a smaller unit)</p> <p>RECORD (measurement equivalents in a two-column table)</p> <p>SOLVE (word problems using the four operations including simple fractions and decimals)</p> <p>SOLVE (word problems requiring expressing measurements given in larger unit in terms of smaller unit)</p> <p>REPRESENT (measurement quantities using diagrams with a measurement scale)</p> <p>APPLY (area formulas in real world and mathematical problems)</p> <p>APPLY (perimeter formulas in real world and mathematical problems)</p>	<ul style="list-style-type: none"> • Required: <ul style="list-style-type: none"> Daily Warm up sheets (# for the day it is) ○ Related MCAS Questions (can be used as assessments) • Suggested: <ul style="list-style-type: none"> ○ Trailblazers <ul style="list-style-type: none"> ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ <p>OnCore Assessments and Lessons</p>

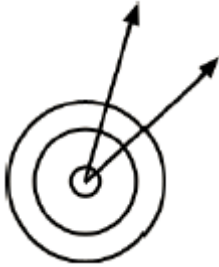

Unit Assessments
<p>The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.</p>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 7 - Exploring Angles and Angle Measurement

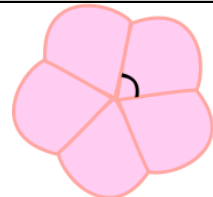
Pacing: 2 weeks

Mathematical Practices
<p><i>Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.</i></p> <p><i>Practices in bold are to be emphasized in the unit.</i></p> <ol style="list-style-type: none">1. Make sense of problems and persevere in solving them.2. Reason abstractly and quantitatively.3. Construct viable arguments and critique the reasoning of others.4. Model with mathematics.5. Use appropriate tools strategically.6. Attend to precision.7. Look for and make use of structure.8. Look for and express regularity in repeated reasoning..
Domain and Standards Overview
<p>Measurement and Data</p> <ul style="list-style-type: none">• Geometric measurement: understand concepts of angle and measure angles.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 7 - Exploring Angles and Angle Measurement

CCSS	Explanations and Examples*
<p>4.MD.5. Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle measurement:</p> <p>a. An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through $\frac{1}{360}$ of a circle is called a “one-degree angle,” and can be used to measure angles.</p> <p>b. An angle that turns through n one-degree angles is said to have an angle measure of n degrees.</p>	<p>4.MD.5. the diagram below will help students understand that an angle measurement is not related to an area since the area between the 2 rays is different for both circles let the angle measure is the same.</p> 
<p>4.MD.6. Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure.</p>	<p>4.MD.6. Before students begin measuring angles with protractors, they need to have some experiences with benchmark angles. They transfer their understanding that a 360° rotation about a point makes a complete circle to recognize and sketch angles that measure approximately 90° and 180°. They extend this understanding and recognize and sketch angles that measure approximately 45° and 30°. They use appropriate terminology (acute, right, and obtuse) to describe angles and rays (perpendicular).</p>
<p>4.MD.7. Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure.</p>	<p>4.MD.7. Examples</p> <ul style="list-style-type: none"> • If the two rays are perpendicular, what is the value of m? • Joey knows that when a clock's hands are exactly on 12 and 1, the angle formed by the clock's hands measures 30°. What is the measure of the angle formed when a clock's hands are exactly on the 12 and 4? • The five shapes in the diagram are the exact same size. Write an 

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 7 - Exploring Angles and Angle Measurement

CCSS	Explanations and Examples*
	<p>equation that will help you find the measure of the indicated angle. Find the angle measurement.</p> 

Concepts What Students Need to Know	Skills What Students Need To Be Able To Do	<u>Required</u> and Suggested Activities
Angles	<p>RECOGNIZE (as geometric shapes that are formed when two rays share common endpoint) UNDERSTAND (concepts of their measurement) MEASURE (in whole number degrees using a protractor) SKETCH (given a specified measure) RECOGNIZE (measures as additive) SOLVE (addition and subtraction problems to find the unknown measures in real world and mathematical problems)</p>	<ul style="list-style-type: none"> • Required: <ul style="list-style-type: none"> Daily Warm up sheets (# for the day it is) ○ Related MCAS Questions (can be used as assessments) • Suggested: <ul style="list-style-type: none"> ○ Trailblazers <ul style="list-style-type: none"> ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ <p>OnCore Assessments and Lessons</p>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 8 - Understanding Properties of Two-Dimensional Figures

Unit Assessments

The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.

Pacing: 3 weeks

Mathematical Practices

Mathematical Practices #1 and #3 describe a classroom environment that encourages thinking mathematically and are critical for quality teaching and learning.

Practices in bold are to be emphasized in the unit.

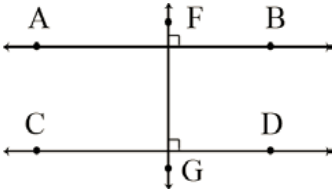


- 1. Make sense of problems and persevere in solving them.**
2. Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.**
4. Model with mathematics.
- 5. Use appropriate tools strategically.**
- 6. Attend to precision.**
- 7. Look for and make use of structure.**
8. Look for and express regularity in repeated reasoning.

Domain and Standards Overview










Geometry

- Draw and identify lines and angles, and classify shapes by properties of their lines and angles.

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 8 - Understanding Properties of Two-Dimensional Figures

CCSS	Explanations and Examples*
<p>4.G.2 Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.</p>	<p>4.G.2. Two-dimensional figures may be classified using different characteristics such as, parallel or perpendicular lines or by angle measurement.</p> <p><u>Parallel or Perpendicular Lines:</u> Students should become familiar with the concept of parallel and perpendicular lines. Two lines are parallel if they never intersect and are always equidistant. Two lines are perpendicular if they intersect in right angles (90°).</p> <p>Students may use transparencies with lines to arrange two lines in as different ways to determine that the 2 lines might intersect in one point or may never intersect. Further investigations may be initiated using geometry software. These types of explorations may lead to a discussion on angles.</p> <p>Parallel and perpendicular lines are shown below:</p> <div style="text-align: center;">  </div> <p>Example: Identify which of these shapes have perpendicular or parallel sides and justify your selection.</p> <div style="text-align: center;">  </div> <p style="text-align: right;">A possible justification that students might give is: A square has perpendicular lines because the sides meet at a corner, forming right angles.</p> <div style="text-align: right;">  </div> <p>Continued on next page</p>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 8 - Understanding Properties of Two-Dimensional Figures

CCSS	Explanations and Examples*
	<p>4.G.2. Continued</p> <p><u>Angle Measurement:</u> This expectation is closely connected to 4.MD.5, 4.MD.6, and 4.G.1. Students' experiences with drawing and identifying right, acute, and obtuse angles support them in classifying two-dimensional figures based on specified angle measurements. They use the benchmark angles of 90°, 180°, and 360° to approximate the measurement of angles.</p> <p>Right triangles can be a category for classification. A right triangle has one right angle. There are different types of right triangles. An isosceles right triangle has two or more congruent sides and a scalene right triangle has no congruent sides.</p>
<p>4.G.3. Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry.</p>	<p>4.G.3. Students need experiences with figures which are symmetrical and non-symmetrical. Figures include both regular and non-regular polygons. Folding cut-out figures will help students determine whether a figure has one or more lines of symmetry.</p>
<p>4.G.1. Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures.</p>	<p>4.G.1. Examples of points, line segments, lines, angles, parallelism, and perpendicularity can be seen daily. Students do not easily identify lines and rays because they are more abstract.</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: left;"> <p>Right angle </p> <p>Acute angle </p> <p>Obtuse angle </p> <p>Straight angle </p> </div> <div style="text-align: left;"> <p> segment</p> <p> line</p> <p> ray</p> <p> parallel lines</p> <p> perpendicular lines</p> </div> </div>

Wilmington Curriculum Design Unit Planner and Pacing Guide
Grade 4 Mathematics
Unit 8 - Understanding Properties of Two-Dimensional Figures

Concepts: What Students Need to Know	Skills: What Students Need To Be Able To Do	Required and Suggested Activities
<p>Two-dimensional Figures</p> <p>Line of Symmetry</p> <p>Geometric Attributes</p> <ul style="list-style-type: none"> • Points • Lines • Line segments • Rays • Angles (right, acute, obtuse) • Perpendicular lines • Parallel lines 	<p>CLASSIFY (based on presence or absence of parallel or perpendicular lines)</p> <p>CLASSIFY (based on presence or absence of angles of a specified size)</p> <p>RECOGNIZE (right triangles)</p> <p>IDENTIFY (right triangles)</p> <p>RECOGNIZE (for two-dimensional figure)</p> <p>IDENTIFY (within figures)</p> <p>DRAW</p> <p>DRAW</p> <p>IDENTIFY (in two-dimensional figures)</p>	<ul style="list-style-type: none"> • Required: <ul style="list-style-type: none"> Daily Warm up sheets (# for the day it is) ○ Related MCAS Questions (can be used as assessments) • Suggested: <ul style="list-style-type: none"> ○ Trailblazers <ul style="list-style-type: none"> ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ ▪ Unit ____ Lesson ____ <p>OnCore Assessments and Lessons</p>

Unit Assessments

The items developed for this section can be used during the course of instruction when deemed appropriate by the teacher.

Grade Four Pacing Guide Supplementary Websites

<http://nsdl.org/commcore/math/?id=4&s=20>

http://fcit.fldoe.org/fcat2/pdf/sample/1112/math/FL530621_Gr4_Math_TB_WT_r3g.pdf - sample questions

http://fcit.fldoe.org/fcat2/pdf/sample/1112/math/FL530622_Gr4_Math_AK_WT_r2g.pdf - sample answers

http://www.eduplace.com/math/mw/tools/tt_4.html - manipulatives

Unit 1:

N/A

Unit 2:

Prime & Composite Numbers

http://alex.state.al.us/lesson_view.php?id=26336 PowerPoint and worksheets

<http://exchange.smarttech.com/search.html?q=Prime%20and%20Composite%20Numbers> SmartBoard Lesson

<http://www.coolmath.com/prealgebra/00-factors-primes/03-prime-composite-numbers-01.htm> Explanation and Practice

<http://teachers.net/lessons/posts/2955.html>

Factors & Multiples

<http://www.mrmaffesoli.com/Printables/4OA4/index.html>

<http://www.uen.org/core/math/downloads/4OA4.pdf>

<http://www.math-play.com/Factors-and-Multiples-Jeopardy/Factors-and-Multiples-Jeopardy.html>

<http://www.youtube.com/watch?v=j9PEQP7gpgE>

http://www.math-aids.com/Factors/List_All_Factors.html

<http://www.collaborativelearning.org/multiplesandfactors.pdf>

<http://www.rundesroom.com/2012/04/still-having-fun-with-factors-and.html>

Patterns with Numbers

<http://www.dadsworksheets.com/v1/Worksheets/Number%20Patterns.html>

<http://www.dadsworksheets.com/v1/Worksheets/Number%20Patterns.html>

<http://www.uen.org/core/math/downloads/4OA5.pdf>

http://www.math-aids.com/Function_Table/

Patterns with Shapes

<http://mathwire.com/problemsolving/4hexagondragons.pdf>

<http://mathwire.com/algebra/butterflies.pdf>

<http://mathwire.com/algebra/growingpatterns.html>

Unit 3:

Multi Step Problems

<http://www.kidzone.ws/math/wordproblems.htm>

<http://www.dadsworksheets.com/v1/Worksheets/Word%20Problems.html>

<http://www.ixl.com/math/grade-4/multi-step-word-problems> (limited access)

<http://www.mathplayground.com/wordproblems.html>

http://www.mathplayground.com/TB_MD/tb_md2_iFrame.html

<http://www.mathplayground.com/gsmbegin.html>

<http://www.beaconlearningcenter.com/WebLessons/CamersonsTrip/default.htm>

http://www.helpingwithmath.com/printables/worksheets/word_problems/4oa3word_problems01.htm

http://www.helpingwithmath.com/printables/worksheets/word_problems/4oa3word_problems02.htm

http://www.softschools.com/quizzes/math/multistep_word_problems/quiz1054.html

http://www.internet4classrooms.com/skill_builders/word_problems_math_fourth_4th_grade.htm

<http://www.prongo.com/farm/game.html>

<http://www.doe.mass.edu/mcas/student/2011/> Access to recent MCAS assessments

<http://www.superteacherworksheets.com/word-problems.html> With space to write an equation representing the problem

<http://www.mathworksheets4kids.com/word-problems.html> A variety of problems across operations

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/reteach.html> Database of worksheets

<http://www.tlsbooks.com/fourthgradeworksheets.htm> Database of worksheets

http://www.softschools.com/quizzes/math/4th_grade_word_problems/quiz682.html Online Word problem quiz with multiple steps

<http://www.onlinemathlearning.com/4th-grade-word-problems.html>

<http://www.superteachertools.com/jeopardyx/jeopardy-review-game.php?gamefile=1320865016> Jeopardy game with word problems

<https://sites.google.com/site/crethirdgrade/word-problems> Database of word problems

<http://www.tvokids.com/games/tumbletownmathletics> Simple game, third stage, good for reading directions

Problem solving processes

<http://www.purplemath.com/modules/translat2.htm>

<http://www.studygs.net/mathproblems.htm>

Unit 4: FRACTIONS

<http://www.mathnstuff.com/math/spoken/here/2class/60/mult.htm>

<http://www.shodor.org/interactivate/lessons/FractionKing/>

<http://www.kidsolr.com/math/fractions.html>

<http://illuminations.nctm.org/LessonDetail.aspx?ID=U113>

<http://illuminations.nctm.org/LessonDetail.aspx?ID=L344>

<http://illuminations.nctm.org/LessonDetail.aspx?ID=L343>

<http://illuminations.nctm.org/LessonDetail.aspx?id=U152>

<http://www.quia.com/cb/95583.html>

http://www.learner.org/courses/learningmath/number/session9/part_a/

<http://www.visualfractions.com/CompareL/comparel.html>

<http://www.uen.org/Lessonplan/preview.cgi?LPid=21524>

<http://www.uen.org/Lessonplan/preview.cgi?LPid=18913>

<http://www.uen.org/Lessonplan/preview.cgi?LPid=21525>

http://www.math-aids.com/Number_Lines/Fractions_Number_Lines.html

<http://aaamath.com/fra.htm>

<http://www.kidsnumbers.com/turkey-terminator-math-game.php>

<http://www.mathfactcafe.com/view/view.aspx?t=P&g=4>

<http://www.education.com/worksheet/article/decimal-dash-practice-ordering-decimals-11/>

DECIMALS

<https://www.teachingchannel.org/videos/elementary-math-lesson-plan>

http://65.61.2.239/lessons/toc_vol12.html

<http://www.uen.org/Lessonplan/preview.cgi?LPid=18916>

<http://www.instructorweb.com/lesson/decimalmoney.asp>

<http://www.moneyinstructor.com/lesson/decimalfraction.asp>

<http://www.moneyinstructor.com/lesson/fracdecimalpercent.asp>

<http://www.teachervision.fen.com/decimals/activity/3153.html>

http://www.math-aids.com/Number_Lines/Decimals_Number_Lines.html

http://www.nsa.gov/academia/_files/collected_learning/elementary/arithmetic/diving_for_decimals.pdf

<http://www.mathsisfun.com/decimals.html>

<http://www.teach-nology.com/worksheets/math/fractions/compare/1/>

http://alex.state.al.us/lesson_view.php?id=23980

http://www.nsa.gov/academia/_files/collected_learning/elementary/arithmetic/diving_for_decimals.pdf

http://www.helpingwithmath.com/by_subject/place_value/pla_place_value08.htm

http://www.teachervision.fen.com/tv/printables/Math_5_PS_2-10.pdf

http://www.lessonpathways.com/Pathways/Detail?path=%2F05_Math%2FYear_5_Math_Guided_Journey%2F21Fractions_Decimals_and_Number_Lines

<http://www.teachingideas.co.uk/maths/decnolines.htm>

http://www.math-aids.com/Number_Lines/Decimals_Number_Lines.html

<http://www.homeschoolmath.net/worksheets/decimal.php>

<http://aaamath.com/dec.htm>

<http://decimalsquares.com/dsGames/>

<http://www.math-salamanders.com/decimal-place-value-worksheets.html>

<http://www.education.com/worksheets/decimals/>

<http://www.tulyn.com/4th-grade-math/decimals/wordproblems>

Unit 5:

Fraction Resources:

<http://mail.clevelandcountyschools.org/~ccselem/FOV1-000411E2/4th%20Fractions%20Unit.pdf?Plugin=Lof>

(80 pages of activities and lessons that correlate to common core)

Equivalent Fractions

4.nf.1

<http://fractionbars.com/CommonCore/Gd4Les/CCSSLes4Gd4.pdf> (lesson)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSWkSh4aGd4.pdf> (worksheet 1)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSWkSh4bGd4.pdf> (worksheet 2)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-equivalent-1.pdf> (worksheet0

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-equivalent-2.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-equivalent-3.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-equivalent-4.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-equivalent-5.pdf> (worksheet)

Addition and Subtraction

4.nf.3b

<http://fractionbars.com/CommonCore/Gd4Les/CCSSJoinSeptParts.pdf> (lesson)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSJoinSepPartsWkShGd4.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-addition-1.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-addition-2.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-addition-3.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-addition-4.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-subtraction-1.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-subtraction-2.pdf> (worksheet)

<http://www.kidsknowit.com/free-educational-worksheets/download-worksheets/math-fractions-subtraction-3.pdf> (worksheet)

<http://www.dadsworksheets.com/v1/Worksheets/Fraction%20Addition.html> (website with many worksheets)

<http://www.dadsworksheets.com/v1/Worksheets/Fraction%20Subtraction.html> (website with many worksheets)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r8-1.pdf> (worksheet)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r8-3.pdf> (worksheet)

Mixed Numbers

4.nf.3c

<http://fractionbars.com/CommonCore/Gd4Les/CCSSAddSubtMixed.pdf> (lesson)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSAddSubtMixWkShGd4.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF3C/4NF3C-1.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF3C/4NF3C-2.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF3C/4NF3C-3.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF3C/4NF3C-LIM1.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF3C/4NF3C-LIM2.pdf> (worksheet)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r7-4.pdf> (worksheet)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r8-2.pdf> (worksheet)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r8-4.pdf> (worksheet)

Word Problems using Fractions

4.nf.3d

<http://www.mrmaffesoli.com/Printables/4NF3D/4NF3D-1.pdf> (game)

<http://www.mrmaffesoli.com/Printables/4NF3D/4NF3D-2.pdf> (worksheet)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r8-5.pdf> (worksheet)

<http://www.mathworksheets4kids.com/word-problems/fractions/like-addition.pdf> (worksheet)

Multiplication

<http://www.mrmaffesoli.com/Printables/4NF4/4NF4-1.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF4/4NF4-2.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF4/4NF4-3.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF4/4NF4-4.pdf> (worksheet)

<http://www.mrmaffesoli.com/Printables/4NF4/4NF4-5.pdf> (worksheet)

<http://www.dadsworksheets.com/v1/Worksheets/Fraction%20Multiplication.html>

(website with many worksheets)

4.nf.4a

<http://fractionbars.com/CommonCore/Gd4Les/CCSSMultiWholeUnitFracGd4.pdf> (lesson)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSWholeTimesUnitWkShGd4.pdf> (worksheets)

4.nf.4b

<http://fractionbars.com/CommonCore/Gd4Les/CCSSMultiStep1Gd4.pdf> (lesson)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSMultiWkSh72Gd4.pdf> (worksheet 1)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSMultiWkSh73Gd4.pdf> (worksheet 2)

4.nf.4c

<http://fractionbars.com/CommonCore/Gd4Les/CCSSWholeTimesFrac.pdf> (lesson)

<http://fractionbars.com/CommonCore/Gd4WkSh/CCSSWordProbWkShGd4.pdf> (worksheet)

Fractions using a line plot

4.md.4

<http://schools.utah.gov/CURR/mathelem/Core-Curriculum/Measurment---Data/4MD4.aspx> (lesson)

Unit 6:

Measurement:

<http://www.uen.org/Lessonplan/preview.cgi?LPid=16318>

<http://www.mathworksheetwizard.com/grade4/grade4measurements.html>

<http://www.uen.org/Lessonplan/preview.cgi?LPid=16315>

<http://www.kidsknowit.com/free-educational-worksheets/worksheets.php?worksheet=Metric>

<http://www.kidsknowit.com/free-educational-worksheets/worksheets.php?worksheet=weights-measures-us>

<http://www.dadsworksheets.com/>

<http://www.abcteach.com/directory/basics/math/measurement/>

<http://www.thatquiz.org/tq/previewtest?A/O/Z/P/83711291417153> (some mixed review)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r12-1.pdf>www.primaryresources.co.uk/maths/powerpoint/y4_length_word_probs.ppt (customary measures)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r12-2.pdf> (metric measures)

<http://www.pleasanton.k12.ca.us/lesweb/fourth/enrich/e12-1.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/enrich/e12-2.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/enrich/e12-3.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/enrich/e2-10.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/enrich/e2-11.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/enrich/e3-7.pdf>

Volume:

http://mathandreadinghelp.org/exploring_volume_related_to_4th_grade_math.html

http://www.superteacherworksheets.com/measurement/gallonbot-questions_TWFAQW.pdf

http://www.internet4classrooms.com/grade_level_help/measure_liquids_math_fourth_4th_grade.htm

http://gk12.coe.drexel.edu/modules/doc/Quincy_Brown/Volume_Exercise.pdf

Elapsed Time:

<http://www.charliefrench.com/PDF/Gr4Meas7.pdf>

<http://www.teachervision.fen.com/telling-time/printable/30949.html>

<http://www.studyzone.org/testprep/math4/d/elapsedtime4l.cfm>

<http://www.internet4classrooms.com/elapsed-time.htm>

http://www.superteacherworksheets.com/elapsed-time/elapsedtimechart_TZTTR.pdf

<http://www.mathworksheetwizard.com/grade4/grade4time.html>

<http://www.kidsknowit.com/free-educational-worksheets/worksheets.php?worksheet=Time>

<http://www.dadsworksheets.com/v1/Worksheets.html>

<http://www.mathslice.com/actionctl.php?actionid=512>

http://prek-8.com/2ndgrade/timeWorksheets_index4.php

<http://marg.mhost.com/MathGr5/elapsedtime.htm>

http://www.edhelper.com/Telling_Time_Word_Problems.htm

Money

<http://www.mathworksheets4kids.com/word-problems/decimals/addition.pdf>

<http://www.mathworksheets4kids.com/word-problems/decimals/subtraction.pdf>

<http://www.mathworksheets4kids.com/word-problems/decimals/multiplication.pdf>

<http://www.mathworksheets4kids.com/word-problems/decimals/division.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r9-6.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r2-12.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r4-7.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r4-8.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r9-11.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r12-3.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/enrich/e2-12.pdf>

Unit 7:

Parallel and Perpendicular:

<http://www.dadsworksheets.com/v1/Worksheets/Basic%20Geometry.html>

http://www.homeschoolmath.net/teaching/g/parallel_and_perpendicular.php

Circle Angles - <http://www.uen.org/Lessonplan/preview.cgi?LPid=18973>

Right Angles-<http://www.uen.org/Lessonplan/preview.cgi?LPid=6106>

Half-Circle Protractor- <http://www.uen.org/Lessonplan/preview.cgi?LPid=21520>

Unit 8:

Parallel and Perpendicular

<http://www.dadsworksheets.com/v1/Worksheets/Basic%20Geometry.html>

http://www.homeschoolmath.net/teaching/g/parallel_and_perpendicular.php

<http://www.studyzone.org/testprep/math4/d/lines4l.cfm>

http://www.internet4classrooms.com/grade_level_help/classify_lines_segments_geometry_math_third_3rd_grade.htm

http://www.mathlearningcenter.org/media/Bridges_Gr4_OnlineSupplement/B4SUP-C1_GeomParallel_0409.pdf

Acute and Obtuse Angles

<http://www.dadsworksheets.com/v1/Worksheet>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r11-1.pdf>

<http://www.khanacademy.org/math/geometry/angles/v/acute-right-and-obtuse-angles>

<http://www.greatschools.org/worksheets-activities/5680-acute-and-obtuse-angles.gs>

<http://www.rhymerocker.com/classifying-angles-worksheets.html>

Right Triangles

http://www.nsa.gov/academia/_files/collected_learning/elementary/geometry/Classifying_Triangles.pdf

<http://www.mathworksheets4kids.com/triangles/name-angles.pdf>

<http://www.pleasanton.k12.ca.us/lesweb/fourth/reteach/r11-3.pdf>

http://www.mathsisfun.com/right_angle_triangle.html